

FREE BODY DIAGRAM:-

⇒ A body is said to be 'free' when it is singled out from other bodies for the purposes of dynamic (or) static Analysis.

⇒ To represent all known and unknown, Reactions, Tension, Thrust acting on a body under a system of forces through a diagram, called FBD.

\* procedure to Draw FBD :-

- ⇒ Separate the body from its surrounding
- ⇒ Draw all known & unknown forces acting on body.
- ⇒ Find all reactions, Horizontal and vertical components, Tension, and Thrust.

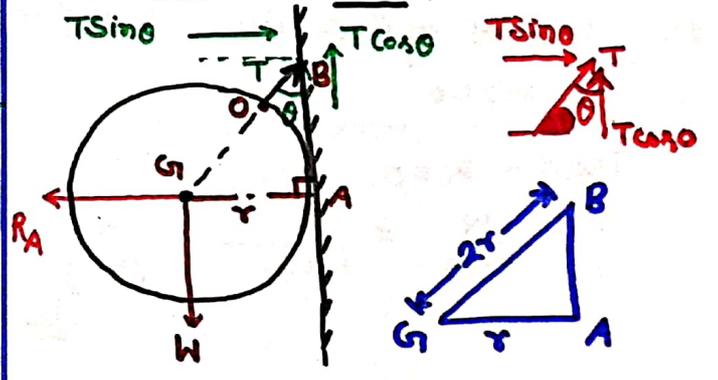
- Draw all angles of sides, arms etc.
- Write all Geometrical relations.

Question:- [B.T.E.U.P. 1990]

A sphere is hanging with the help of a rope from a smooth vertical wall. The weight of the sphere is (W). Length of the rope is equal to the radius of sphere. Then find-

- (1) Tension in the rope.
- (2) Its inclination from vertical.
- (3) Reactions of sphere on wall.

Given data:



- Weight of  $W$  is acting on  $C$ .
- $R_A$   $\perp$  to wall, along  $AC$ .
- $T$  in rope along  $CB$ .

According to question-

$$OB = OC = AC = r$$

$$\angle BAC = 30^\circ$$

(ii) Consider  $\Delta BAC$ .

$$\sin \theta = \frac{CA}{CB} = \frac{r}{2r} = \frac{1}{2}$$

$$\theta = \sin^{-1}\left(\frac{1}{2}\right)$$

$$\boxed{\theta = 30^\circ} \text{ Ans.}$$

(i) In General equ<sup>m</sup> Condition-

$$\sum Y = 0$$

$$T \cos \theta - W = 0$$

$$\left\{ T = \frac{W}{\cos \theta} = \frac{W}{\cos 30^\circ} = \frac{2W}{\sqrt{3}} \right\} \text{ Ans.}$$

(iii) Similarly for equilibrium condition-

$$\sum X = 0$$

$$T \sin \theta - R_A = 0$$

$$R_A = T \sin \theta = T \times \sin 30^\circ = T \times \frac{1}{2}$$

$$R_A = \frac{T}{2} = \frac{\frac{2W}{\sqrt{3}}}{2} = \frac{2W}{\sqrt{3}} \times \frac{1}{2}$$

$$\left[ R_A = \frac{W}{\sqrt{3}} \right] \text{ Ans.}$$

Hence;

$$\left\{ T = \frac{2W}{\sqrt{3}} ; \theta = 30^\circ ; R_A = \frac{W}{\sqrt{3}} \right\} \text{ Ans.}$$